PAPER
Improving the Secure Electronic Transaction Protocol by Using Signcryption**

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#### Abstract

SUMMARY In the past few years, we have seen the emergence of a large number of proposals for electronic payments over open networks. Among these proposals is the Secure Electronic Transaction (SET) protocol promoted by MasterCard and VISA which is currently being deployed world-widely. While SET has a number of advantages over other proposals in terms of simplicity and openness, there seems to be a consensus regarding the relative inefficiency of the protocol. This paper proposes a lightweight version of the SET protocol, called "LITESET." For the same level of security as recommended in the latest version of SET specifications, LITESET yields a $56.2 / 51.4 \%$ reduction in the computational time in message generation/verification and a $79.9 \%$ reduction in communication overhead. This has been achieved by the use of a new cryptographic primitive called signcryption. We hope that our proposal can contribute to the practical and engineering side of real-world electronic payments. key words: signcryption, SET, computational overhead, message overhead


## 1. Introduction

There is a growing demand for global electronic payments. The Secure Electronic Transaction (SET) protocol is being regarded as one of the important candidates. However, straightforward implementation of SET may impose heavy computation and message overhead on a system that employs SET, primarily due to its use of the RSA digital signature and encryption scheme [9]. This article makes an attempt to improve the efficiency of SET by using a new cryptographic technology called signcryption [10], which simultaneously fulfills both the functions of digital signature and public-key encryption in a logically single step. We show how to incorporate signcryption into SET, and evaluate the efficiency of our implementation. Our improved SET will be called "LITESET" or a light-weight

[^0]Secure Electronic Transaction protocol.
Detailed analysis and comparison shows that LITESET provides a $56.2 \%$ reduction in the computational time in message generation, a $51.4 \%$ reduction in the computational time in message verification, and a $79.9 \%$ reduction in communication overhead.

Section 2 gives a brief review of the SET protocol. Problems with the efficiency of SET are summarized in Sect.3. Section 4 proposes an adaptation of signcryption for SET. Our LITESET protocol is also specified in the same section. This is followed by Sect. 5 where significant improvements of LITESET over SET are presented. Section 6 closes the paper with some concluding remarks.

## 2. An Overview of SET

The payment model on which SET is based consists of three participants: a cardholder, a merchant, and a payment gateway. The card holder $(C)$ initiates a payment with the merchant $(M)$. The merchant then has to authorize the payment; the payment gateway acts as the front end to the existing financial network, and through this the card issuer can be contacted to explicitly authorize each and every transaction that takes place. In the SET protocol, there are in total 32 different types of messages [6]. These messages are summarized in Table 1. Among the messages, the most important ones and transmitted at the highest frequency are the following six [5], [7]: PInitReq, PInitRes, PReq, PRes, AuthReq and AuthRes. Other messages are used mainly for administrative purposes, such as creating certificates, canceling messages, registration, error handling etc. Hence these messages are transmitted with significantly smaller frequency than the above mentioned six messages, which in turn implies that any attempt to improve the efficiency of SET must focus on the six main messages. The flow of the six main messages is shown in Fig. 1.

Next we discuss in detail the functions of the six dominant messages. A few frequently used notations are summarized in Table 2.

The SET protocol starts with Purchase Initialization (implementation of PInitReq and PInitRes is shown in Table 3). Purchase Request is then executed conforming to the structure described in Table 4. In

Table 1 SET messages.

| PInitReq,PInitRes | Purchase initialization request/response. |
| :--- | :--- |
| PReq,PRes | Purchase request/response. |
| AuthReq,AuthRes | Authorization request/response. |
| AuthRevReq, <br> AuthRevRes | Authorization reversal request/response. |
| InqReq,InqRes | Inquiry request/response. |
| CapReq,CapRes | Capture request/response. |
| CapRevReq, <br> CapRevRes | Capture reversal request/response. |
| CredReq,CredRes | Credit request/response. |
| CredRevReq, <br> CredRevRes | Credit reversal request/response. |
| PCertReq,PCertRes | Payment gateway's certificate <br> request/response. |
| BatchAdminReq, <br> BatchAdminRes | Batch Administration request/response. |
| CardCInitReq, <br> CardCInitRes | Cardholder's certificate initialization <br> request/response. |
| Me-AqCInitReq, <br> Me-AqCInitRes | Merchant's or acquirer's certificate <br> initialization request/response. |
| RegFormReq, <br> RegFormRes | Registration form request/response. |
| CertReq,CertRes | Certificate request/response. |
| CertInqReq, <br> CertInqRes | Certificate inquiry request/response. |



Fig. 1 Flows of the main SET messages.

Table 2 Notations.

| $E_{k}(t)$ | to encrypt $t$ by using a key $k$. |
| :---: | :--- |
| $D_{k}(t)$ | to decrypt $t$ by using a key $k$. |
| $H(t)$ | to hash $t$. |
| $P v_{e}$ | participant $e$ 's private key. |
| $P b_{e}$ | participant $e$ 's public key. |

PReq, PI and OI are destined to different entities but sent in the same cryptographic envelope. They share a signature called dual signature [6], [7] which can be verified by either entity. Dual signature used in SET is constructed as illustrated in Table 4.

After receiving PReq, the merchant verifies it (especially, Dual signature). If it is valid, he produces AuthReq and sends it to the payment gateway $(P)$. AuthRseq includes AuthReqData and PI, where PI is copied from PReq.

Upon receiving AuthReq, the payment gateway

Table 3 Structure of PInitReq/Res.

| message | message factor |
| :---: | :---: |
| PInitReq | \{RRPID,LID-C,Chall_C,BrandID,BIN $\}$ |
| PInitRes | \{PInitResData, $E_{P v_{M}}(H($ PInitResData) $)\}$ |
| RRPID | UniqueID for one pair of <br> request and response. |
| LID-C | LocalID of cardholder's transaction. |
| Chall_C | Cardholder's challenge. |
| BIN | Cardholder's account number. |
| PInitResData | \{TransID,RRPID, <br> Chall_C, Chall_M,PEThumb $\}$ |
| TransID | TransactionID. |
| Chall_M | Merchant's challenge. |
| BrandID | Brand of card. |
| PEThumb | Thumbprint of payment gateway <br> public key certificate. |

Table 4 Structure of PReq.

| message | message factor |
| :---: | :---: |
| PReq | \{PI,OI\} |
| PI | $\left\{E_{P b_{P}}(k\right.$, PANData, nonce $)$, $E_{k}($ PI-OILink,$H$ (PANData,nonce $)$, Dual signature $\}$ |
| OI | \{ OIData, $H$ (PIData) $\}$ |
| PANData | Primary account number data. |
| PIData | Purchase instruction data. |
| OIData | Order information data. |
| PI-OILink | \{PIData(except PANData), $H$ (OIData) $\}$ |
| Dual signature | $E_{P v_{C}}\{H$ (H(PIData), $H$ (OIData) $)$ \} |

verifies it. If successful, the payment gateway sends AuthRes back to the merchant. AuthRes includes CapToken and AuthResData, which shows the state of the transaction. If the verification of AuthReq fails, only

Table 7 Parameters for LITESET messages.

| $K H_{k}(t)$ | to hash $t$ with a key $k$. |
| :---: | :--- |
| $p$ | a large prime. |
| $q$ | a large prime factor of $p-1$. |
| $g$ | an integer in $[1, \cdots, p-1]$ with order q modulo p. |

## 4. LITESET-A Light-Weight Version of SET

In this section, we will show how to improve SET in terms of efficiency: specifically, how to adapt signcryption for SET. The most important part of this work is how to link a message to another message. In our improvement, there are two kinds of efficient linking: LinkedData and CoupledData. The details appear in the following subsection.

### 4.1 Difficulty of Applying Signcryption to SET

As it is well known, since signcryption executes completely different two procedures simultoneously, there often occur several problems in the implementations of certain secrity systems. In SET, the problem of straightforwardly applying signcryption is as follows: signcryption dose not provide efficient message linking though this function is very often required in SET. For example, in PReq the relationship between the informtion for the payment and that for the order must be guaranteed. Namely, PIData and OIData are linked with each other in the message. In conventional SET, this requirement is fulfilled by the dual signature. However, it is very difficult to provide the same property of the dual signature by signcryption for the above reason; alghouth a dual signature can be veirfied by both the merchant and the payment gateway, a signcrypted message cannot be (assuming usual computational costs). Therefore, straightforwardly applied signcryption is not suitable for SET. Hence, in order to apply signcryption to SET we need to construct modified signcryption schemes which provide the function of message linking. In this section, we show the modified signcryptions which fulfill two kinds of message linking in SET.

### 4.2 Notation

Table 7 shows the parameters which are used in this paper (notice that $E_{x}(t), D_{x}(t), H(t), P v_{e}$ and $P b_{e}$ are defined in Table 2). We define the public key of entity $e$ as $P b_{e}=g^{P v_{e}} \bmod p$.

### 4.3 LinkedData

In SET, we often find a situation where the sender (S) has to

- sign the message $M_{1}$,
- encrypt it with the recipient $(R)$ 's public key,
- and show the relationship between $M_{1}$ and certain $M_{2}$.

In conventional SET, to satisfy such demands, $H\left(M_{2}\right)$ is attached to $M_{1}$, and these messages are signed by using $S$ 's private key and then encrypted by using $R$ 's public key. Then, $R$ can verify the linking between $M_{1}$ and $M_{2}$ by checking the value of $H\left(M_{2}\right)$. Namely, if someone falsifies $M_{2}, R$ can find that $M_{2}$ is falsified.

For efficient application of signcryption scheme, we use hashed $M_{2}$ in the verification of the signcrypted $M_{1}$. These linked messages are referred to as LinkedData.

Now let us proceed by showing how to construct LinkedData. The message to be sent by $S$ to $R$ is LinkedData ${ }_{S, P b_{R}}\left(M_{1}, M_{2}\right)$ which is composed as follows:

- LinkedData ${ }_{S, P b_{R}}\left(M_{1}, M_{2}\right)$
$=\left\{L S C_{S, P b_{R}, M_{2}}\left(M_{1}\right), M_{2}\right\}$
where $L S C_{S, P b_{R}, M_{2}}\left(M_{1}\right)=\{r, s, c\}$, and $r, s, c$ are defined by:

$$
x \in_{R}[1, \cdots, q-1]_{r}
$$

$$
\left(k_{1}, k_{2}\right)=H\left(P b_{R}^{x} \bmod p\right)
$$

$r=K H_{k_{1}}\left(H\left(M_{1}\right), H\left(M_{2}\right)\right)$
$s=\frac{x}{r+P v_{S}} \bmod q$
$c=E_{k_{2}}\left(M_{1}\right)$
On receiving LinkedData ${ }_{S, P b_{R}}\left(M_{1}, M_{2}\right), R$ verifies it as follows:

1. $\left(k_{1}, k_{2}\right)=H\left(\left(P b_{S} \cdot g^{r}\right)^{s \cdot P v_{R}} \bmod p\right)$
2. $M_{1}=D_{k_{2}}(c)$
3. If $r=K H_{k_{1}}\left(H\left(M_{1}\right), H\left(M_{2}\right)\right), \quad R$ accepts $M_{1}, M_{2}$.
Accordingly, in order to be able to verify the message $M_{1}$, unfalsified $H\left(M_{2}\right)$ is required. Thus, if someone falsifies $M_{2}, R$ can detect that it is indeed falsified. As examples, AuthReq and AuthRes can be described as LinkedData.

### 4.4 CoupledData

Generally, dual signature is used for linking two messages whose recipients are different. Thus, although one recipient can only see the contents of the message $M_{1}$ he receives, he can be confident of the digest $H\left(M_{2}\right)$ of the other message $M_{2}$. Hence, if one recipient wants to confirm the linking of the two messages, the two recipients send dual signatures $E_{P v_{S}}\left(H\left(H\left(M_{1}\right), H\left(M_{2}\right)\right)\right)$, messages and message digests they received to a reliable institution. By using them and sender's public key, the reliable institution can detect a dishonest act. If $D_{P b_{S}}$ (dual signature) is not identical to $H\left(H\left(M_{1}\right), H\left(M_{2}\right)\right)$ which is made from components sent by one recipient, the reliable institution knows this recipient forged $M_{1}$ and/or $H\left(M_{2}\right)$. And, if dual signatures are valid and $M_{1}$ (or $M_{2}$ ) which is received by one recipient is not hashed to be $H\left(M_{1}\left(\right.\right.$ or $\left.\left.M_{2}\right)\right)$ which is received by the other recipient, the reliable institution
knows the sender conducted a dishonest act.
Here we show how to realize the function of dual signature by applying signcryption. Let the messages which are linked by using this scheme be called CoupledData.

When $S$ sends PReq to $R, S$ must

- sign the messages, $M_{1}$ and $M_{2}$,
- encrypt only $M_{1}$ by using $R^{\prime}$ 's public key,
- send $M_{1}$ and $M_{2}$ to $R$,
- let $R$ send $M_{1}$ to $R^{\prime}$ with keeping $M_{1}$ unread,
- and show the relationship between $M_{1}$ and $M_{2}$ where $R^{\prime}$ is the true recipient of $M_{1}$. In SET, $C$ acts $S, M$ acts $R$, and $P$ acts $R^{\prime}$.

In our implementation, $S$ send CoupledData $a_{S, P b_{R^{\prime}}}$ $\left(M_{1}, M_{2}\right)$ to $R$ as follows:

```
- CoupledData \({ }_{S, P b_{R^{\prime}}}\left(M_{1}, M_{2}\right)=\left\{C S C_{S, P b_{R^{\prime}}, M_{2}}\right.\)
    \(\left.\left(M_{1}\right), \operatorname{CSig}_{S, M_{1}}\left(M_{2}\right)\right\}\)
    \(\diamond \operatorname{CSig}_{S, M_{1}}\left(M_{2}\right)=\left\{s_{1}, r_{1}, M_{2}, H\left(M_{1}\right)\right\}\)
        \(x_{1} \in_{R}[1, \cdots, q-1]\)
        \(r_{1}=H\left(g^{x_{1}}, H\left(M_{1}\right), H\left(M_{2}\right)[, e t c]\right)\)
        \(s_{1}=\frac{x_{1}}{r_{1}+P v_{S}} \bmod q\)
        Upon receiving CoupledData \({ }_{S, P b_{R^{\prime}}}\left(M_{1}, M_{2}\right)\),
        \(R\) verifies it as follows:
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            1. \(\left(g^{x_{1}}\right)=H\left(\left(P b_{S} \cdot g^{r_{1}}\right)^{s_{1}} \bmod p\right)\)
            2. If \(r_{1}=H\left(g^{x_{1}}, H\left(M_{1}\right), H\left(M_{2}\right)[, e t c]\right)\),
                \(R\) accepts \(M_{2}\), and sends \(C S C_{S, P b_{R^{\prime}}, M_{2}}\)
                \(\left(M_{1}\right)\) and \(H\left(M_{2}\right)\) to \(R^{\prime}\).
    \(\diamond C S C_{S, P b_{R^{\prime}}, M_{2}}\left(M_{1}\right)=\left\{r_{2}, s_{2}, c_{2}\right\}\)
        \(x_{2} \in_{R}[1, \cdots, q-1]\)
        \(\left(k_{1}, k_{2}\right)=H\left(P b_{R^{\prime}}^{x_{2}} \bmod p\right)\)
        \(r_{2}=K H_{k_{1}}\left(H\left(M_{1}\right), H\left(M_{2}\right)[, e t c]\right)\)
        \(s_{2}=\frac{x_{2}}{r_{2}+P v_{S}} \bmod q\)
        \(c_{2}=E_{k_{2}}\left(M_{1}\right)\)
        \(R^{\prime}\) verifies \(C S C_{S, P b_{R^{\prime}}, M_{2}}\left(M_{1}\right)\) as follows:
            1. \(\left(k_{1}, k_{2}\right)=H\left(\left(P b_{S} \cdot g^{r_{2}}\right)^{s_{2} \cdot P v_{R^{\prime}}} \bmod p\right)\)
            2. \(\left\{M_{1}\right\}=D_{k_{2}}\left(c_{2}\right)\)
            3. If \(r_{2}=K H_{k_{1}}\left(H\left(M_{1}\right), H\left(M_{2}\right)[, e t c]\right)\),
                \(R^{\prime}\) accepts \(M_{1}\).
    If $S$ wants to designate the recipient of the message, $S$ should put the recipient's public key in etc.

If $S$ wants to encrypt $M_{2}, S$ should send CoupledData as follows:

- CoupledData ${ }_{S, P b_{R^{\prime}}, P b_{R}}\left(M_{1}, M_{2}\right)=\left\{C S C_{S, P b_{R^{\prime}}, M_{2}}\right.$ $\left.\left(M_{1}\right), C S C_{S, P b_{R}, M_{1}}\left(M_{2}\right)\right\}$

$$
\begin{aligned}
& \diamond C S C_{S, P b_{R}, M_{1}}\left(M_{2}\right)=\left\{s_{1}, r_{1}, c_{1}\right\} \\
& \quad x_{1} \in_{R}[1, \cdots, q-1] \\
& \quad\left(k_{3}, k_{4}\right)=H\left(P b_{R} x_{1} \bmod p\right) \\
& s_{1}=\frac{x_{1}}{r_{1}+P v_{S}} \bmod q \\
& r_{1}=K H_{k_{3}}\left(H\left(M_{1}\right), H\left(M_{2}\right)[, e t c]\right) \\
& c_{1}=E_{k_{4}}\left(M_{1}\right) \\
& R \text { verifies } C S C_{S, P b_{R}, M_{1}}\left(M_{2}\right)=\left\{s_{1}, r_{1}, c_{1}\right\} \text { as } \\
& \quad \text { follows: }
\end{aligned}
$$

Table 8 Message structures of LITESET for main messages.

| message | message structure |
| :---: | :---: |
| PInitReq | \{RRPID,LID-C,Chall_C,BrandID,BIN\} |
| PInitRes | \{ $\operatorname{Sig}_{M}$ (PInitResData) \} |
| PReq | $\begin{aligned} & \text { \{CoupledData } \left.a_{C, P b_{P}} \text { (PIData,OIData) }\right\} \\ & \text { If OIData is encrypted, } \\ & \text { \{CoupledData } a_{C, P b_{P}, P b_{M}} \text { (PIData,OIData), } \\ & H(\text { PIData })\} \end{aligned}$ |
| AuthReq | $\begin{aligned} & \left\{\text { LinkedData }{ }_{M, P b_{P}}\right. \text { (AuthReqData, } \\ & \left.\left.\left\{C S C_{S, P b_{P}, \text { OIData }}(\text { PIData }), H(\text { OIData })\right\}\right)\right\} \end{aligned}$ |
| AuthRes | $\left\{\right.$ LinkedData ${ }_{P, P b_{M}}$ (AuthResData, CapToken) $\}$ |
| PRes | $\left\{\operatorname{Sig}_{M}\left(\right.\right.$ PResData) ${ }^{\text {a }}$ |

1. $\left(k_{3}, k_{4}\right)=H\left(\left(P b_{S} \cdot g^{r_{1}}\right)^{s_{1} \cdot P v_{R}} \bmod p\right)$
2. $\left\{M_{2}\right\}=D_{k_{4}}\left(c_{1}\right)$
3. If $r_{1}=K H_{k_{3}}\left(H\left(M_{1}\right), H\left(M_{2}\right)[, e t c]\right), R$ accepts $M_{1}$ (of course, $S$ has to send $H\left(M_{1}\right)$ with CoupledData ${ }_{S, P b_{R^{\prime}}, P b_{R}}$ $\left.\left(M_{1}, M_{2}\right)\right)$, and should send $C S C_{S, P b_{R^{\prime}}, M_{2}}\left(M_{1}\right)$ and $H\left(M_{2}\right)$.
Although dishonest acts are detected in almost the same way as in dual signature scheme, there exist several differences. (1) recipient's private keys are required for detection. (2) although the two recipients can be confident that they have received the same signature in the conventional SET, recipients cannot be confident of the signature which is received by the other recipient in our scheme. With our scheme, more computational costs need to be invested to detect dishonest acts. However, as the need of detection of dishonest acts should arise in very rare situations, we believe that the extra computational costs for detecting dishonest acts with our scheme should not be a disadvantage in practice.

### 4.5 Messages in LITESET

Embodying LinkedData and CoupledData in SET results is a light weight version of the protocol called LITESET. For the six main messages, LinkedData is adapted to AuthReq $\left(\left(M_{1}, M_{2}\right)=(\right.$ AuthReqData, $\mathrm{PI})$ ) and AuthRes $\left(\left(M_{1}, M_{2}\right)=\right.$ (AuthResData, CapToken)), and CoupledData is adapted to PReq $\left(\left(M_{1}, M_{2}\right)=\right.$ (PIData, OIData) $)$. Moreover, to sign only, such as PInitRes and PRes, SDSS1 [10] is adapted to such messages. Accordingly, the six main messages in LITESET are described in Table 8.

For other messages, operations mentioned above are adapted appropriately to their message type, employing a similar approach. A detailed description of these messages is shown in Table A•1. Here, we show only their structure, and message factors in them are not discussed.

## 5. LITESET vs. SET

LITESET relies for its security on the computational infeasibility of the discrete logarithm problem. As-
suming the difficulty of computing the discrete logarithm, the signcryption scheme embodied in LITESET has been proven secure against adaptively chosen ciphertext attacks (the most powerful attacks that one can conceive in the real world) [8], [11]. This means the security level of LITESET is same as the conventional SET with optimal asymmetric encryption padding(OAEP) [1]. Similar to the original SET protocol, the LITESET protocol is secure in practice.

The rest of this section is devoted to a detailed comparison of the efficiency of LITESET and SET. Here, we compare LITESET with SET based on RSA, which is the most common implementation. Of course elliptic cryptosystems are known as quite efficient cryptographical technologies. Signcryption on elliptic curves [12] has been already proposed, and we can realize LITESET on elliptic curves easily. Therefore, we also evaluate the performance of LITESET on elliptic curves.

### 5.1 Computational Costs

The computational cost depends mainly on modulo exponentiations in encryption or signature generation. Hence, the number of modulo multiplications in modulo exponentiation can be used as the computational cost. We estimate the number of modulo multiplications by using "square-and-multiply" and "simultaneous multiple exponentiation." Namely, the number of modulo multiplications for one $g^{x}$ or $P b_{e}{ }^{x}$ is $1.5 \cdot|q|$, and for $\left(P b_{e_{1}} \cdot g^{r}\right)^{s \cdot P v_{e_{2}}}$ it is equal to $\frac{7}{4} \cdot|q|$. In conventional SET, 1024 bit RSA composite is used. To achieve the same security level, $|q|=160$ bit and $|p|=1024$ bit should be chosen for our scheme [10]. Table 9 shows the costs of message generation and verification for the six main messages. We can see that the computational costs are saved over $50 \%^{\dagger}$. For other messages, Table A• 2 shows the costs of message generation and verification, respectively, where we can also see the significant cost reduction. Note that LITESET can be

[^1]applied to almost all of the computers and that we do not assume any specifed computers. The actual time depends on the particular computer used in SET and LITESET. As an example, on M16C processor [13] the computational time for PReq generation in the conventional SET is estimated to be 10 sec approximately. Therefore, that in LITESET becomes 5 sec on the same processor. Additionally, we roughly estimate the performance of LITESET on elliptic curves, assuming that the computational cost for elliptic curve crypto systems is $1 / 10$ of that for the conventional discrete-logarithm based cryptosystems. In Table 10, the computational cost of LITESET on elliptic curves is shown. The cost reduction can be considered as significant.

In a most probable situation, cardholder's computer is much slower than merchant's and payment gateway's. Hence, the efficiency depends largely on the load on cardholder's computer. Our proposal reduces this load significantly; PReq(generation), PInitRes(verification) and PRes(verification) are managed on cardholder's computer, and their computational costs are saved as much as $37.0 \%$.

Table 9 Computational cost for message generation/verification of main messages (discrete-logarithm based LITESET).

| message | conventional <br> scheme | our scheme | saving |
| :---: | :---: | :---: | :---: |
| PInitReq | $-/-$ | $-/-$ | $-/-$ |
| PInitRes | $384 / 384$ | $240 / 280$ | $37.5 \% / 27.1 \%$ |
| PReq | $768 / 384$ | $480 / 280$ | $37.5 \% / 27.1 \%$ |
| AuthReq | $768 / 1536$ | $240 / 560$ | $68.7 \% / 63.5 \%$ |
| AuthRes | $1536 / 768$ | $480 / 280$ | $68.7 \% / 63.5 \%$ |
| PRes | $384 / 384$ | $240 / 280$ | $37.5 \% / 27.1 \%$ |
| Total | $3840 / 3456$ | $1680 / 1680$ | $56.2 \% / 51.4 \%$ |

Table 10 Computational cost for message generation/verification of main messages (LITESET on elliptic curves).

| message | conventional <br> scheme | our scheme <br> on elliptic curves | saving |
| :---: | :---: | :---: | :---: |
| PInitReq | $-/-$ | $-/-$ | $-/-$ |
| PInitRes | $384 / 384$ | $24 / 28$ | $93.7 \% / 92.7 \%$ |
| PReq | $768 / 384$ | $48 / 28$ | $93.7 \% / 92.7 \%$ |
| AuthReq | $768 / 1536$ | $24 / 56$ | $96.9 \% / 96.3 \%$ |
| AuthRes | $1536 / 768$ | $48 / 28$ | $96.9 \% / 96.3 \%$ |
| PRes | $384 / 384$ | $24 / 28$ | $93.7 \% / 92.7 \%$ |
| Total | $3840 / 3456$ | $168 / 168$ | $95.6 \% / 95.1 \%$ |

On the implementaion on IC cards, since coprocessors are well-optimized for modulo multiplication, modulo division, e.g., $s$ in LinkedData, is not desirable. However, in LITESET the number of modulo divisions is significantly smaller than that of modulo multiplications. Hence, we consider that the inefficiency of the modulo division can be ignored.

### 5.2 Message Overhead

In our evaluation, digital signature and public key encrypted session key are regarded as message overhead. Namely, for our scheme, $r(|r|=80$ bit $), s(|s|=160$ bit $)$ and hashed variables $(|H(t)|=160 \mathrm{bit})$ for message linking are message overhead. Table 11 shows the message overhead of the six main messages. We see that message overhead is saved over $70 \%$ for each message. Table A•3 shows the message overhead of other messages; hence the reduction of message overhead is also significant. Note that in LITESET on elliptic curves the message overhead is same as that in the discrete-logarithm based LITESET.

### 5.3 Future Parameters

We should also consider situations that require larger security parameters. On account of the continuing developments in computer technologies, we will certainly need larger security parameters in the future. Even at the present time, we can often reach specific situations that the payment should be done more safely. Table 12 shows the advantage of LITESET over RSA-based SET with larger parameters. Here, LITESET's advantage is estimated by using the average computational cost and message overhead for six main messages assuming

Table 11 Message overhead of main messages.

| message | conventional <br> scheme | our scheme | saving |
| :---: | :---: | :---: | :---: |
| PInitReq | - | - | - |
| PInitRes | 1024 bit | 320 bit | $68.7 \%$ |
| PReq | 2008 bit | 720 bit | $64.1 \%$ |
| AuthReq | 4056 bit | 640 bit | $84.2 \%$ |
| AuthRes | 4256 bit | 480 bit | $88.7 \%$ |
| PRes | 1024 bit | 320 bit | $68.7 \%$ |
| Total | 12368 bit | 2480 bit | $79.9 \%$ |

Table 12 Saving in computational cost (for message generation/verification) and message overhead of LITESET over the RSA-based SET for future parameters.

| $\|p\|=\|n\|$ | $\|q\|$ | $\|K H(\cdot)\|$ | computational cost for <br> message generation/verification | message <br> overhead |
| :---: | :---: | :---: | :---: | :---: |
| 1024 bit | 160 bit | 80 bit | $56.2 \% / 51.4 \%$ | $79.9 \%$ |
| 1536 bit | 176 bit | 88 bit | $67.9 \% / 64.4 \%$ | $85.4 \%$ |
| 2048 bit | 192 bit | 96 bit | $73.7 \% / 70.8 \%$ | $88.0 \%$ |
| 3072 bit | 224 bit | 112 bit | $79.6 \% / 77.3 \%$ | $90.7 \%$ |
| 4096 bit | 256 bit | 128 bit | $82.5 \% / 80.6 \%$ | $92.0 \%$ |
| 5120 bit | 288 bit | 144 bit | $84.2 \% / 82.5 \%$ | $92.8 \%$ |
| 8192 bit | 320 bit | 160 bit | $89.1 \% / 87.8 \%$ | $95.0 \%$ |

different security parameters. We can find that LITESET's advantage will be more significant in the future.

## 6. Conclusion

In this paper, a new and very practical method which reduces computational cost and message overhead of SET messages is proposed based on signcryption. In SET, messages are often signed, encrypted and linked to other messages. With the help of signcryption, all of these functions are fulfilled, but with a far smaller cost than that required by SET. In the future, security parameters will be larger to compensate advances in cryptanalysis, and the advantages of our proposed LITESET over the current version of SET, based on RSA, will be more significant.

## Acknowledgments

We would like to thank Chandana Gamage and Kanta Matsuura for their help in preparing this paper.

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## Appendix A: Signcryption, SDSS1 and RSA with OAEP

This appendix is intended to give a brief summary of signcryption [10], a shortened digital signature scheme called SDSS1 [10], and the RSA with OAEP scheme [1], [9]. The reader is directed to the original references for further details of the schemes.

## A. 1 Signcryption

Signcryption is a new cryptographic technology that can reduce computational cost and message overhead by using an idea to manage digital signature and public key encryption simultaneously. For example, it can be implemented as follows [10]. We define the public key of an entity $e$ as $P b_{e}=g^{P v_{e}} \bmod p$. When the sender $(S)$ sends a message to the $\operatorname{recipient}(R), S$ sends the message in a signcrypted form $S C_{S, P b_{R}}($ message $)=$ $r, s, c$ where

- $x \in_{R}[1, \cdots, q-1]$
$\left(k_{1}, k_{2}\right)=H\left(P b_{R}^{x} \bmod p\right)$
$r=K H_{k_{1}}(H($ message $))$
$s=\frac{x}{r+P v_{S}} \bmod q$
$c=E_{k_{2}}$ (message)
On receiving $S C_{S, P b_{R}}$ (message), $R$ verifies it as follows:

1. $\left(k_{1}, k_{2}\right)=H\left(\left(P b_{S} \cdot g^{r}\right)^{s \cdot P v_{R}} \bmod p\right)$
2. message $=D_{k_{2}}(c)$
3. If $r=K H_{k_{1}}(H$ (message $)$ ), $R$ accepts message.

## A. 2 SDSS1-A Shortened Digital Signature Scheme

SDSS1 proposed in [10] is an improvement of DSS [4]. If $S$ wants to sign message, $S$ sends $\operatorname{Sig}_{S}$ (message) as follows:

- $\operatorname{Sig}_{S}($ message $)=\{s, r$, message $\}$
$x \in_{R}[1, \cdots, q-1]$
$s=\frac{x}{r+P v_{S}} \bmod q$
$r=H\left(g^{x}\right.$, message $)$
$R$ verifies $\operatorname{Sig}_{S}($ message $)=\{s, r$, message $\}$ as follows:

1. $\left(g^{x}\right)=H\left(\left(P b_{S} \cdot g^{r}\right)^{s} \bmod p\right)$
2. If $r=H$ ( $g^{x}$, message $)$, $R$ accepts message.

## A. 3 The RSA with OAEP Cryptosystem

Suppose $n_{S}$ is the enough large composite with factoring difficulty, $S$ calculates two integers $e_{S}$ and $d_{S}$ each having roughly the same size and satisfying $e_{S} d_{S}=$ $1 \bmod \lambda\left(n_{S}\right)$, where $\lambda()$ is the Carmichael function. Then, $S$ uses $\left(e_{S}, n_{S}\right)$ for $S$ 's public key and $\left(d_{S}\right)$ for $S$ 's private key. $S$ 's signature on message is defined as $s=H(\text { message })^{d_{S}} \bmod n_{S}$. Other user can verify whether $s$ is $S$ 's valid signature on message by checking whether $H$ (message) is identical to $s^{e_{S}} \bmod n_{S}$.

Similarly to $S, R$ can create $R$ 's public key $\left(e_{R}, n_{R}\right)$ and secret key $d_{R}$. Let $G$ and $F$ be random oracles $G$ : $\{0,1\}^{k_{0}} \rightarrow\{0,1\}^{n+k_{1}}$ and $F:\{0,1\}^{n+k_{1}} \rightarrow\{0,1\}^{k_{0}}$, respectively, where $n=\mid$ message-encryption key $\mid$ and $n+k_{0}+k_{1}=\left|n_{R}\right|$. To send message to $R$ in a secure way, $S$ picks random message-encryption key $k$ and calculates $z=\left(k \| 0^{k_{1}}\right) \oplus G(r)$, where $r$ is a $k_{0}$-bit random number. Then $S$ sends to $R c_{1}=E_{k}$ (message) and $c_{2}=\{z \|(r \oplus F(z))\}^{e_{R}} \bmod n_{R}$. Upon receiving $c_{1}$ and $c_{2}, R$ can retrieve $k$ by calculating $z=$ $\left[c_{2}{ }^{d_{R}} \bmod n_{R}\right]^{n+k_{1}}, r=\left[c_{2}{ }^{d_{R}} \bmod n_{R}\right]_{k_{0}} \oplus F(z)$ and $k=[z \oplus G(r)]^{n}$, employing it he can decrypt $c_{1}$.

## Appendix B: Evealuation of Other Messages

In this appendix, we show message structures, computational cost and message overhead of LITESET messages except for the main six messages. Table A•1, Table A• 2 and Table A. 3 show the message structure, the computational cost and the message overhead, respectively.

Table A•1 Message structures of LITESET for other messages.
$\left.\begin{array}{|l|l|}\hline \text { message } & \text { structure } \\ \hline \text { AuthRevReq } & \begin{array}{l}\{\text { LinkedData } \\ \text { \{PI,CapToken }\} \text { ) }\}\end{array}\end{array}\right\}$

Table A• 2 Computational cost for message generation/verification for other messages (discrete-logarithm based LITESET).

| message | conventional <br> scheme | our scheme | saving |
| :---: | :---: | :---: | :---: |
| AuthRevReq | $768 / 1536$ | $240 / 560$ | $68.7 \% / 63.5 \%$ |
| AuthRevRes | $768 / 768$ | $240 / 280$ | $68.7 \% / 63.5 \%$ |
| CapReq | $768 / 768$ | $240 / 280$ | $68.7 \% / 63.5 \%$ |
| CapRes | $768 / 768$ | $240 / 280$ | $68.7 \% / 63.5 \%$ |
| CapRevReq | $768 / 768$ | $240 / 280$ | $68.7 \% / 63.5 \%$ |
| CapRevRes | $768 / 768$ | $240 / 280$ | $68.7 \% / 63.5 \%$ |
| CredReq | $768 / 768$ | $240 / 280$ | $68.7 \% / 63.5 \%$ |
| CredRes | $768 / 768$ | $240 / 280$ | $68.7 \% / 63.5 \%$ |
| CredRevReq | $768 / 768$ | $240 / 280$ | $68.7 \% / 63.5 \%$ |
| CredRevRes | $768 / 768$ | $240 / 280$ | $68.7 \% / 63.5 \%$ |
| PCertReq | $384 / 384$ | $240 / 280$ | $68.7 \% / 27.1 \%$ |
| PCertRes | $384 / 384$ | $240 / 280$ | $68.7 \% / 27.1 \%$ |
| BatchAdminReq | $768 / 768$ | $240 / 280$ | $68.7 \% / 63.5 \%$ |
| BatchAdminRes | $768 / 768$ | $240 / 280$ | $68.7 \% / 63.5 \%$ |
| CardCInitReq | $-/-$ | $-/-$ | $-/-$ |
| CardCInitRes | $384 / 384$ | $240 / 280$ | $68.7 \% / 27.1 \%$ |
| Me-AqCInitReq | $-/-$ | $-/-$ | $-/-$ |
| Me-AqcInitRes | $384 / 384$ | $240 / 280$ | $37.5 \% / 27.1 \%$ |
| RegFormReq | $384 / 384$ | $240 / 280$ | $37.5 \% / 27.1 \%$ |
| RegFormRes | $384 / 384$ | $240 / 280$ | $37.5 \% / 27.1 \%$ |
| CertReq | $768 / 768$ | $240 / 280$ | $68.7 \% / 63.5 \%$ |
| CertRes | $384 / 384$ | $240 / 280$ | $37.5 \% / 27.1 \%$ |
| CertInqReq | $384 / 384$ | $240 / 280$ | $37.5 \% / 27.1 \%$ |
| CertInqRes | $384 / 384$ | $240 / 280$ | $37.5 \% / 27.1 \%$ |

Table A. 3 Message overhead for other messages.

| message | conventional <br> scheme | our scheme | saving |
| :---: | :---: | :---: | :---: |
| AuthRevReq | 6114 bit | 880 bit | $85.6 \%$ |
| AuthRevRes | 4256 bit | 480 bit | $88.7 \%$ |
| CapReq | 2208 <br> $+(2048 \cdot \mathrm{n})$ bit | 240 <br> $+(240 \cdot \mathrm{n}) \mathrm{bit}$ | $\simeq 88.3 \%$ |
| CapRes | 2048 bit | 240 bit | $88.3 \%$ |
| CapRevReq | 2208 <br> $+(2048 \cdot \mathrm{n})$ bit | 240 <br> $+(240 \cdot \mathrm{n})$ bit | $\simeq 88.3 \%$ |
| CapRevRes | 2048 bit | 240 bit | $88.3 \%$ |
| CredReq | 2208 | 240 | $\simeq 88.3 \%$ |
| CredRes | 2048 bit | 240 bit | $88.3 \%$ |
| CredRevReq | 2208 | 240 | $\simeq 88.3 \%$ |
| CredRevRes | 2048 bit | 240 bit | $88.3 \%$ |
| PCertReq | 1024 bit | 320 bit | $68.7 \%$ |
| PCertRes | 1024 bit | 320 bit | $68.7 \%$ |
| BatchAdminReq | 2048 bit | 240 bit | $88.3 \%$ |
| BatchAdminRes | 2048 bit | 240 bit | $88.3 \%$ |
| CardCInitReq | - | - | - |
| CardCInitRes | 1024 bit | 320 bit | $68.7 \%$ |
| Me-AqCInitReq | - | - | - |
| Me-AqcInitRes | 2048 bit | 240 bit | $88.3 \%$ |
| RegFormReq | 1184 bit | 872 bit | $26.4 \%$ |
| RegFormRes | 1024 bit | 320 bit | $68.7 \%$ |
| CertReq | 1528 bit | 240 bit | $84.3 \%$ |
| CertRes | 1024 bit | 320 bit | $68.7 \%$ |
| CertInqReq | 1024 bit | 320 bit | $68.7 \%$ |
| CertInqRes | 1024 bit | 320 bit | $68.7 \%$ |



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[^0]:    Manuscript received January 18, 1999.
    Manuscript revised February 8, 2000.
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    ${ }^{* *}$ An extended abstract of this paper was presented at Third Australasian Conference on Information Security and Privacy (ACISP'98) [3].

[^1]:    ${ }^{\dagger}$ It is difficult to make quantitative analysis of computational costs involved in certificate verification, which heavily depends on the structure of a certification infrastructure employed. Thus, we do not investigate them here.

